

**Paper 4 - Fundamentals of Business
Mathematics and Statistics**

MTP_Foundation_Syllabus2016_Dec2017_Set 1

Paper-4: Fundamentals of Business Mathematics and Statistics

Time Allowed: 3 Hours

Full Marks: 100

The figures in the margin on the right side indicate full marks.

This question paper has two sections.

Both the sections are to be answered subject to instructions given against each.

Section – A

I. (a) Choose the correct answer (9 × 2 = 18)

- (1) If 3, x, 27 are in continued proportion then $x =$ _____
(a) ± 6 (b) ± 9 (c) ± 7 (d) None of these
- (2) At what rate p.a. S.I. will a sum of money double itself in 25 years?
(a) 4% (b) 3% (c) 5% (d) 6%
- (3) Compute C.I. on ₹ 2500 for 1 year at 12% compounded six months –
(a) 309 (b) 390 (c) 300 (d) 290
- (4) A.M. of two integral numbers exceeds their G.M. by 2 and the ratio of the numbers is 1 : 4. Find the numbers.
(a) 5, 20 (b) 1, 4 (c) 2, 8 (d) 4, 16
- (5) Set of even positive integers less than equal to 6 by selector method.
(a) $\{x/x < 6\}$ (b) $\{x/x = 6\}$ (c) $\{x/x \leq 6\}$ (d) None
- (6) If $\log_{10}^2 = 0.3010$ $\log_2^{10} =$ _____
(a) 0.3322 (b) 3.2320 (c) 3.3222 (d) 5
- (7) If ${}^n P_3 = 120$ then $n =$ _____
(a) 8 (b) 4 (c) 6 (d) None of these
- (8) If ${}^r C_{12} = {}^r C_8$ find ${}^{22} C_r$
(a) 213 (b) 321 (c) 231 (d) None of these
- (9) If one roots of the equation $x^2 - 3x + m = 0$ exceeds the other by 5 then the value of M is equal to _____
(a) -6 (b) -4 (c) 12 (d) 18

I. (b) State whether the following statements are true or false (6 × 1 = 6)

- (1) If 15% of x = 20% of y then $x : y = 4 : 3$ ()
- (2) If the terms -1 + 2x, 5, 5+x are is an A.P. then x is 4 ()
- (3) The statement "Equivalent sets are always equal" is true or false ()
- (4) The logarithm of one to any base is zero ()
- (5) ${}^n C_0 = 1$ is true of false ()
- (6) The degree of the equation $3x^5 + xyz^2 + y^3$ is 3 ()

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Answer: I (a)

(1) $\therefore 3, x, 27$ are in continued proportion.

$$\therefore b^2 = ac$$

$$\Rightarrow x^2 = 3(27) = 81$$

$$x = \sqrt{81}$$

$$= \pm 9 \quad (\text{option b})$$

(2) Let the sum be ₹ P

$$\therefore A = ₹^2P, \quad t = 25 \text{ yrs.}$$

$$\therefore A = P \left(\frac{1+rt}{100} \right)$$

$$\Rightarrow 2P = P \left(\frac{1+25r}{100} \right)$$

$$\Rightarrow 1 = \frac{r}{4} \Rightarrow r = 4\%$$

(Option a)

$$(3) \therefore C.I = P \left[\left(1 + \frac{i}{200} \right)^{2n} - 1 \right]$$

$$= 2500 \left[\left(\frac{1+12}{200} \right)^2 - 1 \right]$$

$$= 2500 \left[\left(\frac{212}{200} \right)^2 - 1 \right]$$

$$= 2500 [(1.06)^2 - 1]$$

$$= 2500 (0.1236)$$

$$= ₹309$$

(Option a)

(4) Let the numbers be $x, 4x$

$$\therefore \frac{x+4x}{2} = \sqrt{x(4x)} + 2$$

$$\Rightarrow \frac{5x}{2} = 2x + 2$$

$$\Rightarrow x = 4$$

\therefore The numbers are 4, 16

(Option d)

(5) $\{x/x \leq 6\}$

(Option c)

$$(6) \log_2 10 = \frac{1}{\log_{10} 2} \cdot \frac{1}{0.3010} = 3.3222$$

(Option c)

$$(7) \therefore {}^n P_3 = 120 \Rightarrow \frac{n!}{n-3!} = 120$$

$$\Rightarrow n(n-1)(n-2) = 120 = 6 \times 5 \times 4$$

$$\therefore n = 6$$

(Option c)

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$$(8) \because {}^r C_{12} = {}^r C_8 \Rightarrow r = 12 + 8 = 20.$$

$$\because {}^{22} C_y = {}^{22} C_{20} = \frac{{}^{22} P_y}{y!} = \frac{22 \times 21}{2} = 21 \times 11 = 231$$

(Option c)

$$(9) \because x^2 - 3x + m = 0$$

Let the roots be α , $\alpha + 5$

$$\because \alpha + (\alpha + 5) = 3$$

$$2\alpha = -2$$

$$\alpha = -1$$

\therefore the roots be -1, 4

\therefore Product of roots = M = -4

(Option b)

Answer: I (b)

$$(1) \because \frac{15}{100}(x) = \frac{20}{100}(y)$$
$$\Rightarrow 3x = 4y \Rightarrow x : y = 4 : 3$$

(T)

(2) \because -1 + 2x, 5, 5 + x are in an A. P

$$\Rightarrow 10 = -1 + 2x + 5 + x$$

$$10 = 3x + 4$$

$$3x = 6 \Rightarrow x = 2$$

(F)

(3) The Statement "Equivalent sets are always equal"

(F)

(4) The logarithm of one to any base is zero

(T)

(5) ${}^n C_0 = 1$

(T)

(6) The degree of the equation $3x^5 + xyz^2 + y^3$ in 3

(F)

II. Answer any four questions. Each question carries 4 marks

(4 × 4 = 16)

(1) Monthly income of two persons Ram and Rahim are in the ratio 5 : 7 and their monthly expenditure are in the ratio 7 : 11. If each of them saves ₹ 60/months. Find their monthly income.

(2) Which is better investment - 3% per year compounded monthly (or) 3.2% per simple interest (given that $(1.0025)^{12} = 1.0304$)

(3) Insert 4 arithmetic means between 4 and 324.

(4) Prove that $\frac{\log 3\sqrt{3} + \log \sqrt{8} - \log \sqrt{125}}{\log 6 - \log 5} = \frac{3}{2}$

(5) A question paper is divided into three groups A, B, C which contains 4, 5 and 3 questions respectively. An examinee is required to answer 6 questions taking atleast 2 from A, 2 From B, 1 From C. in how many ways he can answer.

(6) Solve $2x^{-1} + x^{-\frac{1}{2}} = 6$.

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- (9) $x = \frac{31}{6} - \frac{y}{6}$ is the regression equation of
(b) y on x (b) x on y (c) both (d) none
- (10) If an unbiased coin is tossed twice, the probability of obtaining at least one tail is
(a) 0.25 (b) 0.50 (c) 0.75 (d) 1.00
- (11) Two dice are thrown together. The probability that 'the event the difference of nos. shown is 2' is
(a) 2/9 (b) 5/9 (c) 4/9 (d) 7/9
- (12) If $y = a + bx$, then what is the co-efficient of correlation between x and y?
(a) 1 (b) -1 (c) 1 or -1 according as $b > 0$ or $b < 0$ (d) None of these

III. (b) State whether the following statements are true or false (12 × 1 = 12)

- (1) Harmonic mean is based on all the items in a series ()
- (2) Median is a mathematical average ()
- (3) Co-efficient of variation = $\frac{\text{Co-efficient of variation}}{\text{Mean}} \times 100$ ()
- (4) Range is the value of difference between mode and median ()
- (5) If a coin is tossed, then probability of getting two heads is zero ()
- (6) If an unbiased coin is tossed once, then the two events head and tail are mutually exclusive ()
- (7) 10th Percentile is equal to 9th Decile. ()
- (8) Mean deviation can never be negative ()
- (9) The value of correlation co-efficient lies between 0 & 1 ()
- (10) Bivariate data are the data collected for two variables ()
- (11) When all value s are equal, then standard deviation would be zero ()
- (12) As the sample size increase, range tends to decrease ()

Answer: III (a)

- (1) (d)
(2) (b)
(3) (c)
(4) (c)
(5) (b)
(6) (b)
(7) (c)
(8) (c)

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- (9) (b)
- (10) (c)
- (11) (a)
- (12) (c)

Answer: III (b)

- (1) (T)
- (2) (F)
- (3) (F)
- (4) (F)
- (5) (T)
- (6) (T)
- (7) (F)
- (8) (T)
- (9) (F)
- (10) (T)
- (11) (T)
- (12) (F)

IV. Answer any four questions. Each question carries 6 marks

(4 × 6 = 24)

(1) Draw histogram and frequency polygon of the following data:

Wages (₹)	50-59	60-69	70-79	80-89	90-99	100-109	110-119
No. of Employees	8	10	16	14	10	5	2

(2) Find the median and median-class of the data given below:

Class-boundaries	Frequency
15-25	4
25-35	11
35-45	19
45-55	14
55-65	0
65-75	2

(3) The marks obtained by 6 students were 24, 12, 16, 11, 40, 42. Find the Range. If the highest mark is omitted, find the percentage change in the range.

(4) Compute rank correlation from the following table

X	415	434	420	430	424	428
Y	330	332	328	331	327	325

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(5) Given:

Covariance between X and Y = 16

Variance of X = 25

Variance of Y = 16

(i) Calculate co-efficient of correlation between X and Y,

(ii) If arithmetic means of X and Y are 20 and 30 respectively, find regression equation of Y on X.

(iii) Estimate Y when X = 30.

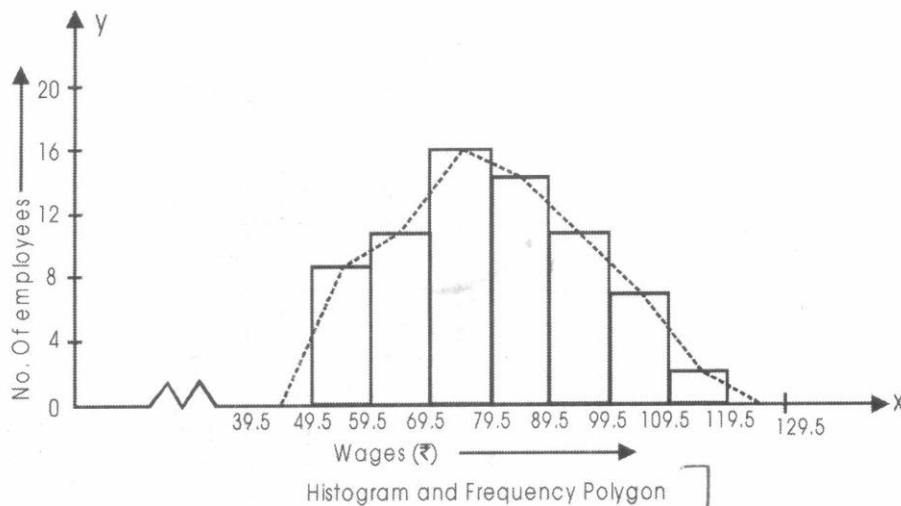
(6) What is the chance that a leap year, selected at random will contain 53 Sundays?

Answer: IV

(1) The variates (wages) are in discrete order, so we are to calculate the class boundaries at first as follows

Class boundaries: 49.5-59.5 59.5-69.5 69.5-79.5 79.5-89.5 89.5-99.5
No. of employees: 8 10 16 14 10

99.5-109.5 109.5-119.5
 5 2



(2) Table: Calculation of Median

Class-boundaries	Frequency	Cumulative frequency
15-25	4	4
25-35	11	15
35-45	19	34
45-55	14	48
55-65	0	48
65-75	2	50 (= N)

Median = Value of $\frac{N}{2}$ item = value of $\frac{50}{2}$ item = value of 25th item, which is greater than cum. Freq. 15. So median lies in the class 35-45.

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Now, Median = $l_1 + \frac{l_2 - l_1}{f} (m - c)$, where $l_1 = 35$, $l_2 = 45$, $f = 19$, $m = 25$, $c = 15$

$$= 35 + \frac{45 - 35}{19} (25 - 15) = 35 + \frac{10}{19} \times 10 = 35 + 5.26 = 40.26$$

Required median is 40.26 and median-class is (35 – 45).

- (3) The marks obtained by 6 students were 24, 12, 16, 11, 40, 42. Find the Range. If the highest mark is omitted, find the percentage change in the range.

Here maximum mark = 42, minimum mark = 11.

$$\therefore \text{Range} = 42 - 11 = 31 \text{ marks}$$

If again the highest mark 42 is omitted, then amongst the remaining. Maximum mark is 40. So, i (revised) = 40 - 11 = 29 marks.

Change in range = 31 - 29 = 2 marks.

$$\therefore \text{Reqd. percentage change} = 2 \div 31 \times 100 = 6.45\%$$

Note: Range and other absolute measures of dispersion are to be expressed in the same unit in which observations are expressed.

For grouped frequency distribution:

In this case range is calculated by subtracting the lower limit of the lowest class interval from the upper limit of the highest.

- (4)

X	R ₁	Y	R ₂	(R ₁ - RR ₂) = D	D ²
415	6	330	3	3	9
434	1	332	1	0	0
420	5	328	4	1	1
430	2	331	2	0	0
424	4	327	5	-1	1
428	3	325	6	-3	9

$$r_k = 1 - \frac{6 \sum D^2}{N(N^2 - 1)}$$

$$= 1 - \frac{1(20)}{6(6^2 - 1)} = 1 - \frac{120}{210} = \frac{210 - 120}{210} = \frac{90}{210} = \frac{3}{7} = 0.429$$

- (5) Given covariance between X and Y = $\frac{\sum XY}{N} = 16$

Variance of X = $\sigma_x^2 = 25$

$$\sigma_x = \sqrt{25} = 5$$

Variance of Y = $\sigma_y^2 = 16$

$$\sigma_y = \sqrt{16} = 4$$

$$\text{Applying formula } r = \frac{\sum XY}{N \sigma_x \sigma_y} = 16$$

$$= \frac{16}{5 \times 4} = 0.8$$

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(ii) Given

$$\bar{X} = 20$$

$$\bar{Y} = 30$$

$$Y - \bar{Y} = r \frac{\sigma_Y}{\sigma_X} (X - \bar{X})$$

$$Y - 6 = 0.9 \frac{1.5}{10} (X - 40)$$

$$Y - 6 = 0.135(X - 40)$$

$$Y - 6 = 0.135 (X - 40)$$

$$Y - 6 = 0.135X - 5.4$$

$$Y = 6 + 0.135X - 5.4$$

$$Y = 0.6 + 0.135X$$

(iii) Put $X = 60$ in regression equation of Y on X .

$$Y = 0.6 + 0.135(60)$$

$$Y = 0.6 + 8.10$$

$$Y = 8.7$$

(6) As a leap year consist of 366 days it contains 52 complete weeks and two more days. The two consecutive days make the following combinations:

- (a) Monday and Tuesday
- (b) Tuesday and Wednesday
- (c) Wednesday and Thursday
- (d) Thursday and Friday
- (e) Friday and Saturday
- (f) Saturday and Sunday, and
- (g) Sunday and Monday

If (f) or (g) occur, then the year consists of 53 Sundays.

Therefore the number of favourable cases = 2

Total number of cases = 7

$$\text{The probability} = \frac{2}{7}$$