Paper 4 - Fundamentals of Business Mathematics and Statistics

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Time Allowed: 3 Hours **Full Marks: 100**

The figures in the margin on the right side indicate full marks.
This question paper has two sections.
Both the sections are to be answered subject to instructions given against each.

Section – A

I. (a) Choose the correct answer **(9 × 2 = 18)**

(1) If 3, x, 27 are in continued proportion then x = _____
(a) ±6 (b) ±9 (c) ±7 (d) None of these

(2) At what rate p.a. S.I. will a sum of money double itself in 25 years?
(a) 4% (b) 3% (c) 5% (d) 6%

(3) Compute C.I. on ₹ 2500 for 1 year at 12% compounded six months –
(a) 309 (b) 390 (c) 300 (d) 290

(4) A.M. of two integral numbers exceeds their G.M. by 2 and the ratio of the numbers is 1 : 4. Find the numbers.
(a) 5, 20 (b) 1, 4 (c) 2, 8 (d) 4, 16

(5) Set of even positive integers less than equal to 6 by selector method.
(a) {x/x<6} (b) {x/x=6} (c) {x/x≤6} (d) None

(6) If $\log_{10}^{2} = 0.3010$ $\log_{2}^{10}$ =____
(a) 0.3322 (b) 3.2320 (c) 3.3222 (d) 5

(7) If ${}^{n}p_{3} = 120$ then n = ___
(a) 8 (b) 4 (c) 6 (d) None of these

(8) If ${}^{r}c_{12} = {}^{r}c_{8}$ find ${}^{22}c_{r}$
(a) 213 (b) 321 (c) 231 (d) None of these

(9) If one roots of the equation $x^2 - 3x + m = 0$ exceeds the other by 5 then the value of M is equal to _____
(a) -6 (b) -4 (c) 12 (d) 18

I. (b) State whether the following statements are true or false **(6 × 1 = 6)**

(1) If 15% of x = 20% of y then x : y = 4 : 3 **( )**

(2) If the terms -1 + 2x, 5, 5+x are is an A.P. then x is 4 **( )**

(3) The statement "Equivalent sets are always equal" is true or false **( )**

(4) The logarithm of one to any base is zero **( )**

(5) ${}^{n}c_{O} = 1$ is true of false **( )**

(6) The degree of the equation $3x^5 + xyz^2 + y^3$ is 3 **( )**

II. Answer any four questions. Each question carries 4 marks (4 × 4 = 16)

(1) Monthly income of two persons Ram and Rahim are in the ratio 5 : 7 and their monthly expenditure are in the ratio 7 : 11. If each of them saves ₹ 60/months. Find their monthly income.

(2) Which is better investment - 3% per year compounded monthly (or) 3.2% per simple interest (given that $(1.0025)^{12} = 1.0304$)

(3) Insert 4 arithmetic means between 4 and 324.

(4) Prove that $\frac{\log 3\sqrt{3} + \log \sqrt{8} - \log \sqrt{125}}{\log 6 - \log 5} = \frac{3}{2}$

(5) A question paper is divided into three groups A, B, C which contains 4, 5 and 3 questions respectively. An examine is required to answer 6 questions taking atleast 2 from A, 2 From B, 1 From C. in how many ways he can answer.

(6) Solve $2x^{-1} + x^{-½} = 6$.

Section - B

III. (a) Choose the correct answer (12 × 2 = 24)

(1) If the co-efficient of correlation between x and y is 2/3 and the standard deviation of x is 3 and standard deviation of y is 4, the covariance between x and y will be _____
(a) 3 (b) 6 (c) 7 (d) 8

(2) Which of the following measures of averages divide the observation into two parts
(a) Mean (b) Median (c) Mode (d) Range

(3) The mode for the series 3, 5, 6, 2, 6, 2, 9, 5, 8, 6 is ……..
(a) 5.1 (b) 5 (c) 6 (d) 8

(4) If Median = 12, Q1 = 6, Q3 = 22 then the co-efficient of Quartile Deviation is _____
(a) 33.33 (b) 60 (c) 66.67 (d) 70

(5) For the observations 6, 4, 1, 6, 5, 10, 4, 8 range is
(a) 10 (b) 9 (c) 8 (d) None

(6) Harmonic mean is used for calculating
(a) Average Growth Rate of variables (b) Average speed of journey
(c) Average rate of increase in net worth of a company (d) All the above 1 to 3

(7) For the regression equation of Y on X, 2x + 3y + 50 = 0. The value of b_{xy} is
(a) 2/3 (b) -2/3 (c) -3/2 (d) None

(8) Two regression lines coincide when
(a) r = 0 (b) r = 2 (c) r = +1 or -1 (d) None

(9) $x = \frac{31}{6} - \frac{y}{6}$ is the regression equation of
(b) y on x (b) x on y (c) both (d) none

(10) If an unbiased coin is tossed twice, the probability of obtaining at least one tail is
(a) 0.25 (b) 0.50 (c) 0.75 (d) 1.00

(11) Two dice are thrown together. The probability that 'the event the difference of nos. shown is 2' is
(a) 2/9 (b) 5/9 (c) 4/9 (d) 7/9

(12) If y = a + bx, then what is the co-efficient of correlation between x and y?
(a) 1 (b) -1 (c) 1 or -1 according as b > 0 or b < 0 (d) None of these

III. (b) State whether the following statements are true or false (12 × 1 = 12)

(1) Harmonic mean is based on all the items in a series ( )

(2) Median is a mathematical average ( )

(3) Co-efficient of variation = $\frac{\text{Co-efficient of variation}}{\text{Mean}} \times 100$ ( )

(4) Range is the value of difference between mode and median ( )

(5) If a coin is tossed, then probability of getting two heads is zero ( )

(6) If an unbiased coin is tossed once, then the two events head and tail are mutually exclusive ( )

(7) 10^{th} Percentile is equal to 9^{th} Decile. ( )

(8) Mean deviation can never be negative ( )

(9) The value of correlation co-efficient lies between 0 & 1 ( )

(10) Bivariate data are the data collected for two variables ( )

(11) When all value s are equal, then standard deviation would be zero ( )

(12) As the sample size increase, range tends to decrease ( )

IV. Answer any four questions. Each question carries 6 marks (4 × 6 = 24)

(1) Draw histogram and frequency polygon of the following data:

Wages (₹)	50-59	60-69	70-79	80-89	90-99	100-109	110-119
No. of Employees	8	10	16	14	10	5	2

(2) Find the median and median-class of the data given below:

Class-boundaries	Frequency
15-25	4
25-35	11
35-45	19
45-55	14
55-65	0
65-75	2

(3) The marks obtained by 6 students were 24, 12, 16, 11, 40, 42. Find the Range. If the highest mark is omitted, find the percentage change in the range.

(4) Compute rank correlation from the following table

X	415	434	420	430	424	428
Y	330	332	328	331	327	325

(5) Given:
Covariance between X and Y = 16
Variance of X = 25
Variance of Y = 16
(i) Calculate co-efficient of correlation between X and Y,
(ii) If arithmetic means of X and Y are 20 and 30 respectively, find regression equation of Y on X.
(iii) Estimate Y when X = 30.

(6) What is the chance that a leap year, selected at random will contain 53 Sundays?