

$$A = \begin{pmatrix} a_{11} & a_{12} & a_{13} \\ a_{21} & a_{22} & a_{23} \\ \vdots & & \end{pmatrix}$$

$$B = \begin{pmatrix} b_{11} & b_{12} \\ b_{21} & b_{22} \\ b_{31} & b_{32} \end{pmatrix}$$

2x3

3x2

Row 1 x Col 1
Row i x Col i
Row 2 x Col 1
Row 3 x Col 2
Row 6 x Col 1

$$AB = \begin{pmatrix} a_{11}b_{11} + a_{12}b_{21} + a_{13}b_{31} \\ a_{11}b_{12} + a_{12}b_{22} + a_{13}b_{32} \\ \vdots \\ a_{11}b_{12} + a_{12}b_{22} + a_{13}b_{32} \end{pmatrix}$$

2x2

Simple Data

Predict

Q1. ✓ How can we use regression? See a simple sample we can import the data

Q2. ✓ How from SPSS? After importing how we can use regression in R.

Q3. After importing how we can use multiple regression in R. we can plot in R.

Q4. How Scatter Diagram



$$y = c + b x$$

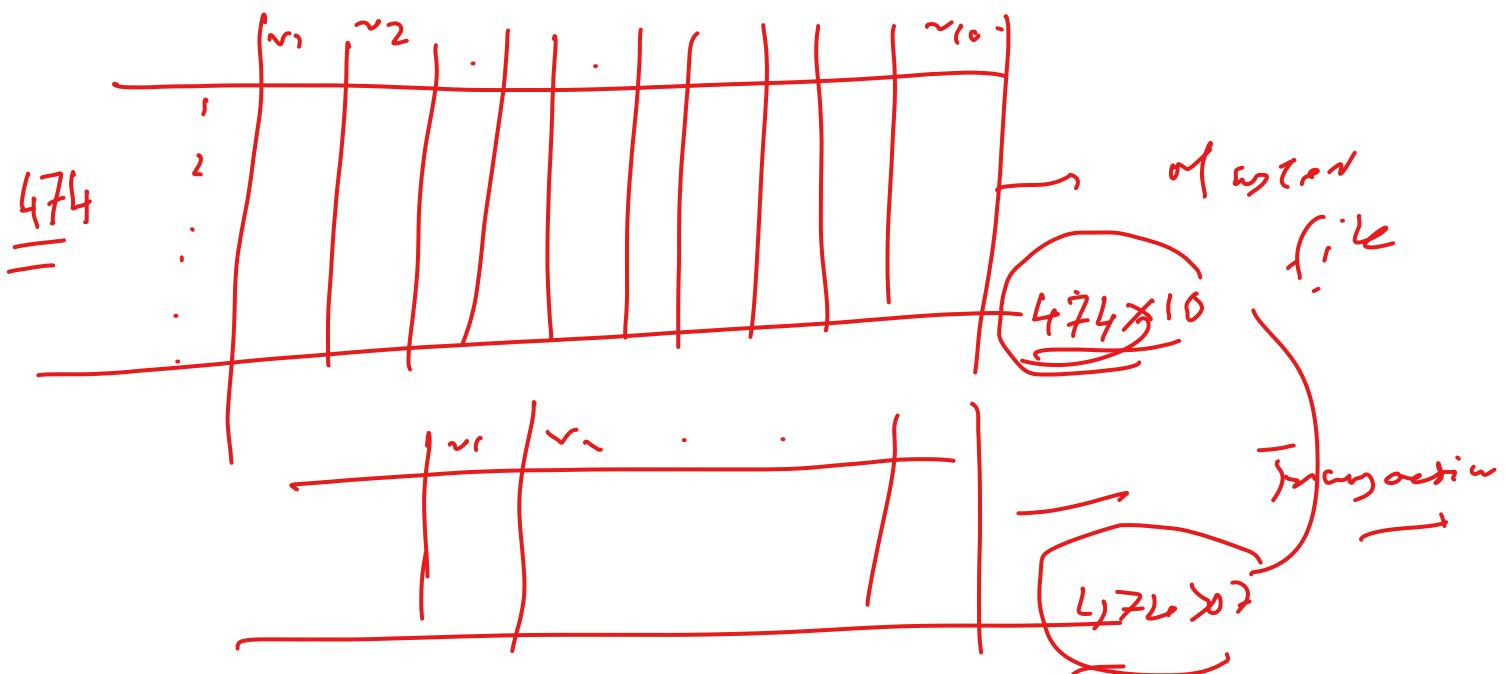
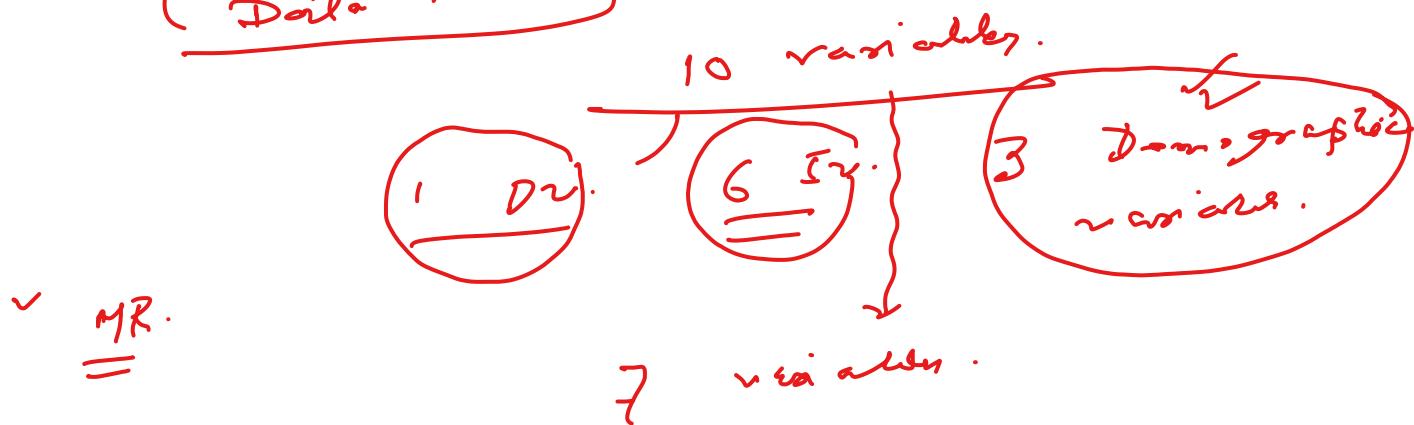
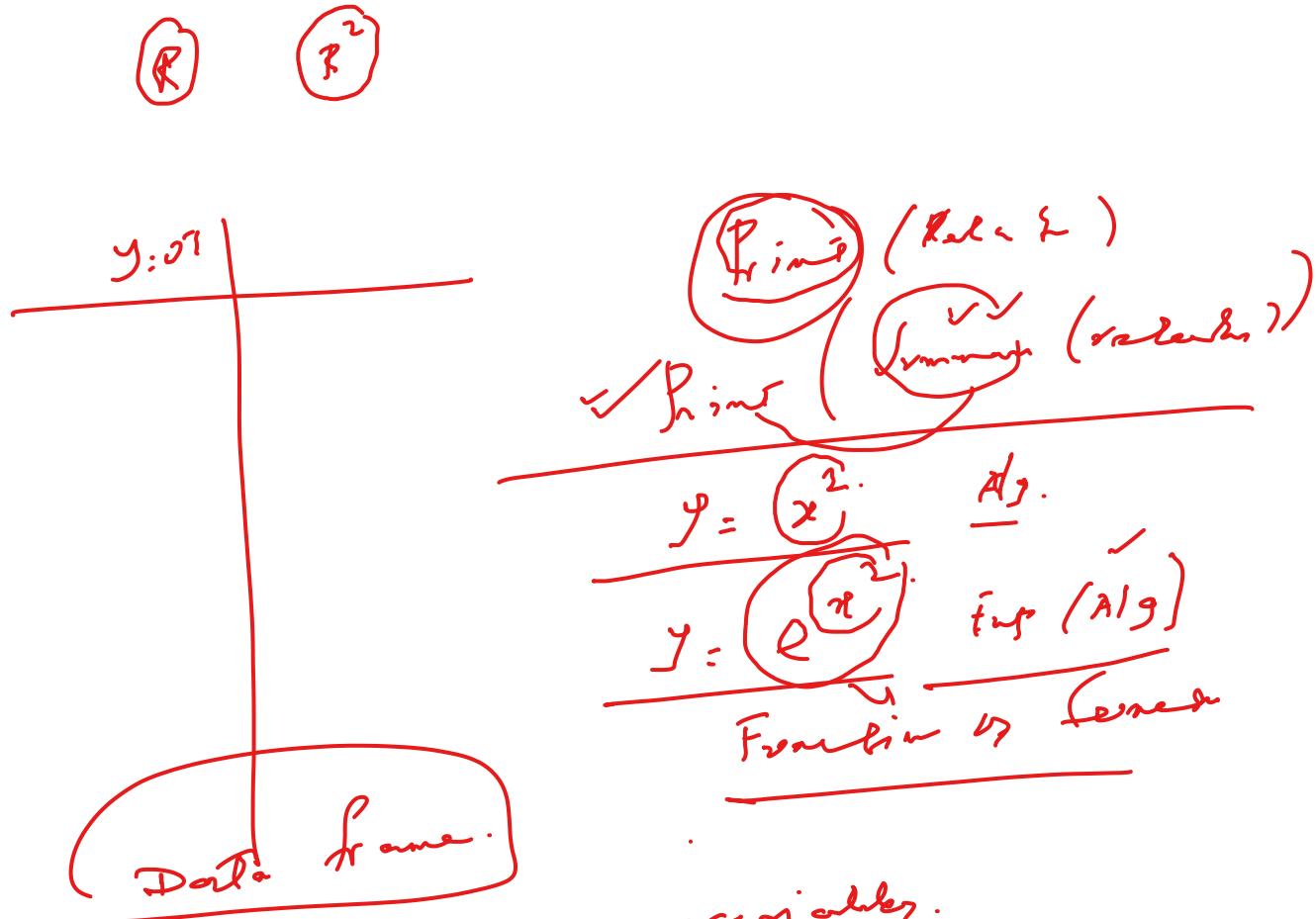
weights = $-38.4551 + 0.6746 \cdot x$

design

tilted right

$$c = -38.4551$$

$$b = 0.6746$$



| y | x |
|-----|-----|
| : | : |
| : | : |
| : | : |
| : | : |
| : | : |

$y = -38.451 + 0.67x$
 we want to predict
 for some given
 values of x .

Initiation

| y | x | $\hat{y} = \{38.45 + 0.67x\}$ | $f_{true} = y - \hat{y}$ | $(Error)^2$ |
|-----|-------|-------------------------------|--------------------------|-------------|
| 63 | Q(15) | ✓ 64. | ✓ | ✓ |
| - | - | ✓ | ✓ | ✓ |
| - | - | ✓ | ✓ | ✓ |
| - | - | ✓ | ✓ | ✓ |
| - | - | ✓ | ✓ | ✓ |

$$R^2 = 1 - \frac{SSE}{TSS}$$

$$\begin{aligned}
 R^2 &= \frac{\sum (Error)^2}{SSE} \\
 TSS &= \sum (y - \bar{y})^2 \\
 &= \sum (y - \hat{y})^2
 \end{aligned}$$

Problem of R^2 .

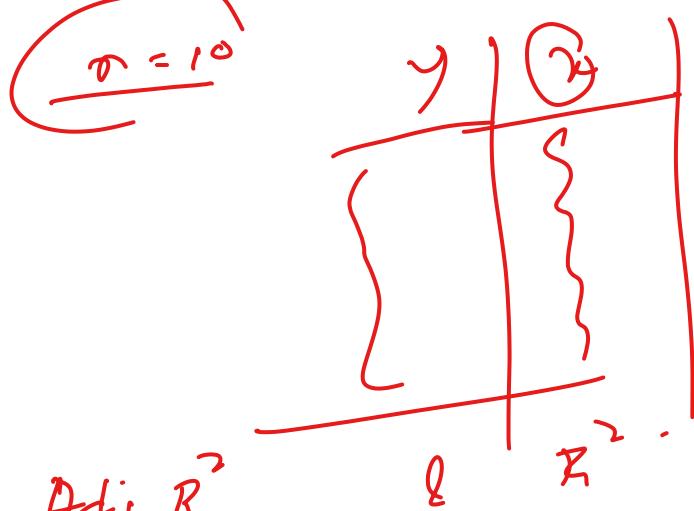
independent of no. of independent variables and no. of observations

Solution modified R^2 = adjusted R^2 .
 with the help of no. of independent variables and no. of observations

$$\text{Adjusted } R^2 = 1 - \frac{\text{SSE}/(n-k-1)}{\text{TSS}/(n-1)}$$

Where $n = \text{no. of observations}$
 $k = \text{indep. variables}$

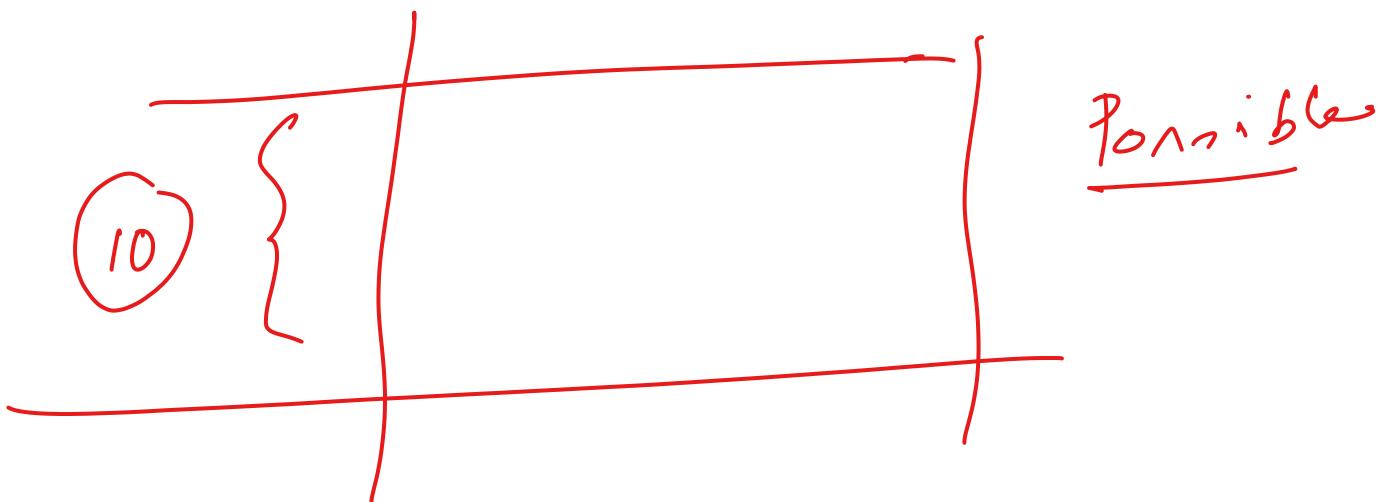
$$\text{Adj } R^2 \leq R^2$$



$$\begin{aligned} \frac{n-k-1}{n-1} &= \text{Degree of freedom} \\ &\text{fraction} \\ n-1 &= D.F. \text{ for TSS} \\ k+1 &= 10-1-1 \\ &= 8 \end{aligned}$$

$$\text{Adj } R^2 = 0.8 \quad \left\{ \begin{array}{l} R^2 = 0.8 \\ Q = 0.6 \end{array} \right\} = 0.2$$

For \dots no. of observations is less.
 $\&$ only one variable is less.
 $\&$ If in less no. of variables = 2



How many df. < no of variables

App/ln. forward stepwise regression

\hat{f}

$\hat{R}^2 \rightarrow$ involving diff.

Degrees of freedom. (DF)

Concept of DF.

DF = no. of independent Parameters.

variables + $x + y + z = 6$

eqn $z = 6 - x - y$

for max $\rightarrow z = f(x, y)$ $z = \text{Dep.}$

$= 2$ $(x=1, y=3) \quad z=3$ $x, y = \text{Ind.}$

$= 6, y=1$ $z=-1$ $\rightarrow DF = 3-1.$

2 4 6 8 5.

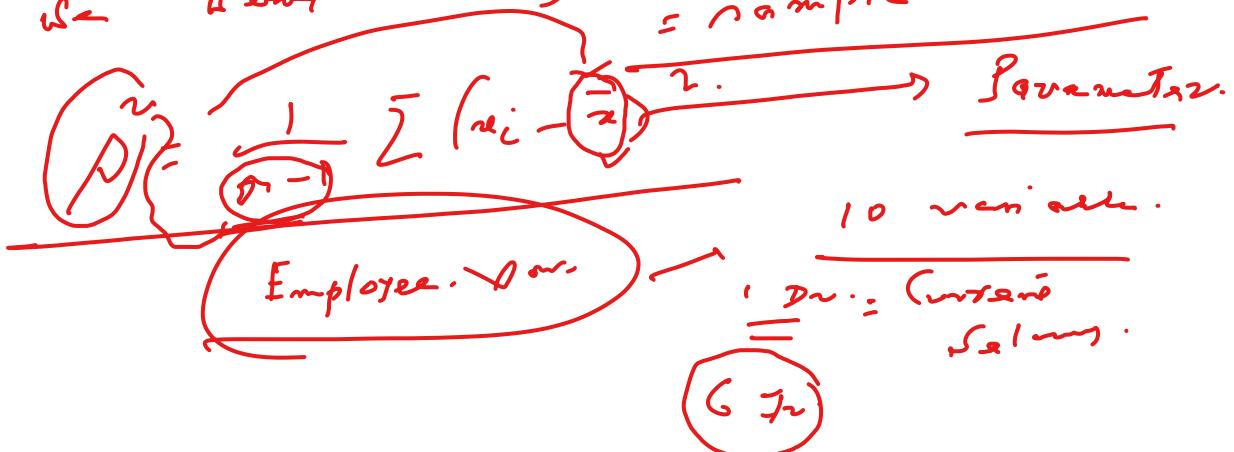
$\bar{x} = \frac{2+4+6+8+5}{5} = 5$

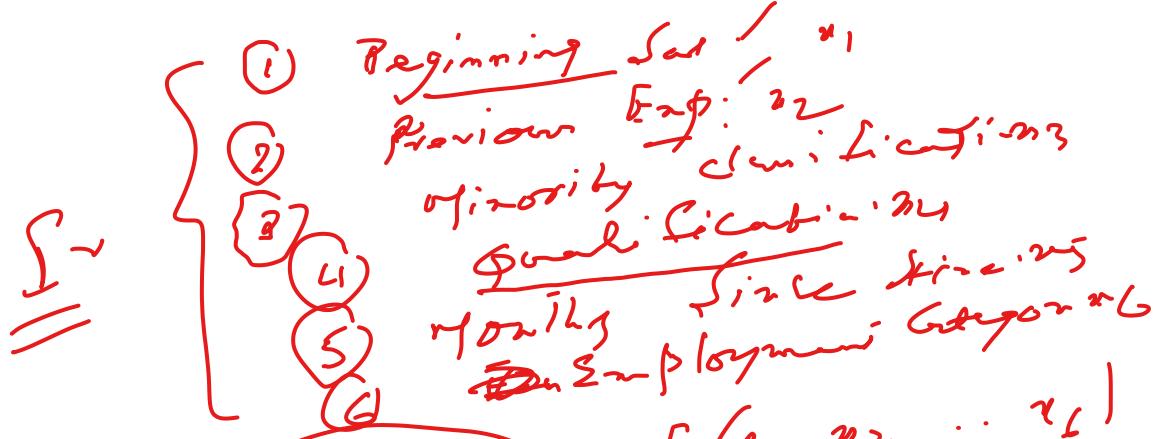
$\bar{x} = \frac{\sum x_i}{n}$

\bar{x} is known

We want to estimate \hat{y} .

\hat{y} = sample variable





Obj. $(\text{Current Role}) = f(x_1, x_2, \dots, x_n)$
 (Obj.) Current Role from Specs.

① Import file from Specs.

$x_1 \sim \text{char.}$ Beg.
 $x_2 \sim \text{numeric.}$ Br. - numeric.
 $x_3 \sim \text{numeric.}$ Tr. - numeric.

Current role
 ↓
 y

Missing Analysis.

F
 ~ NAP.
 ↓
 Not applicable.

HA.
 ↓
 Not available.

DG.
 ↓
 Do not know.

Remark.

| | | | | | | |
|----|---|---|---|---|---|--------------------------|
| R1 | v | - | ~ | - | - | all missing. |
| R2 | v | - | x | x | - | Missing for Col 3, Col 4 |
| | - | 1 | . | . | 1 | |
| | . | . | . | . | . | |
| | - | | | | | |

474

HA → 0 =

