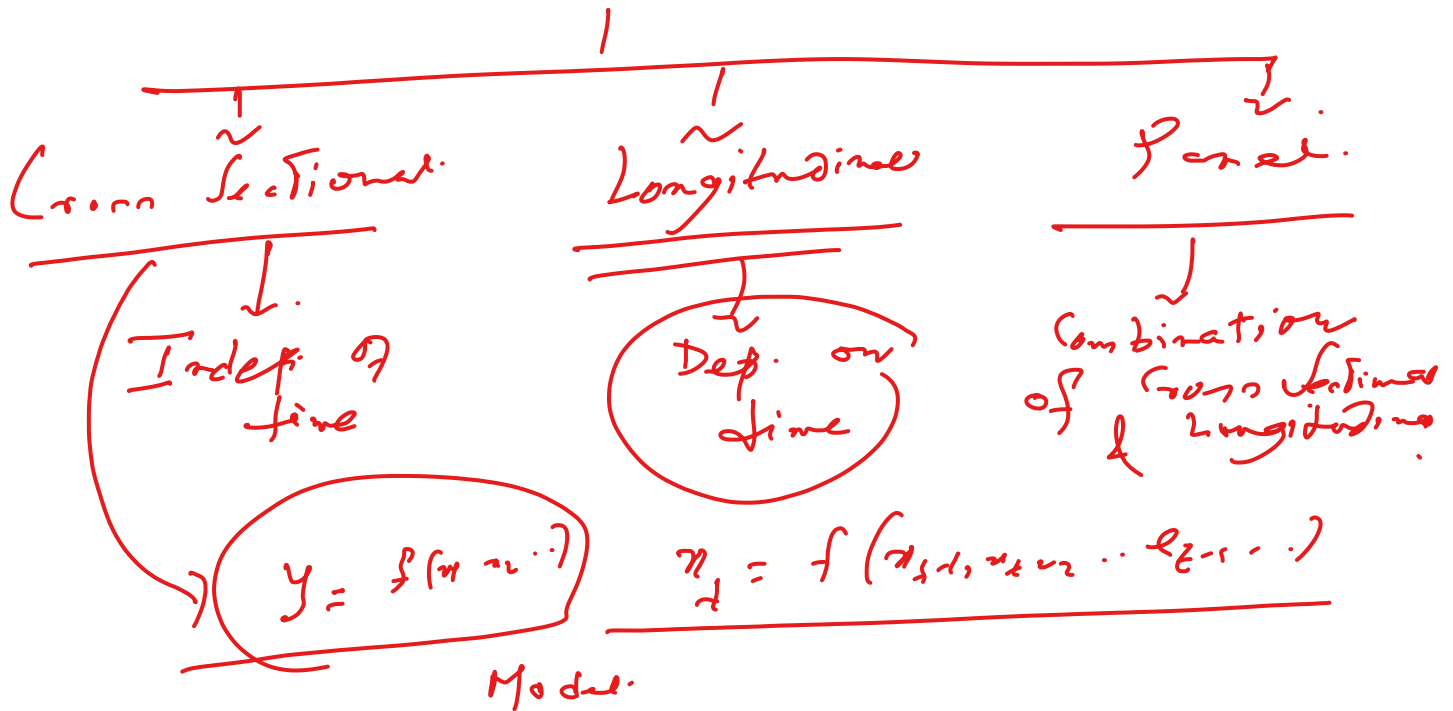


24.04.2022

Model.



Validation

84 months

2015 April. } observed data points (known)
2022 Nov. }

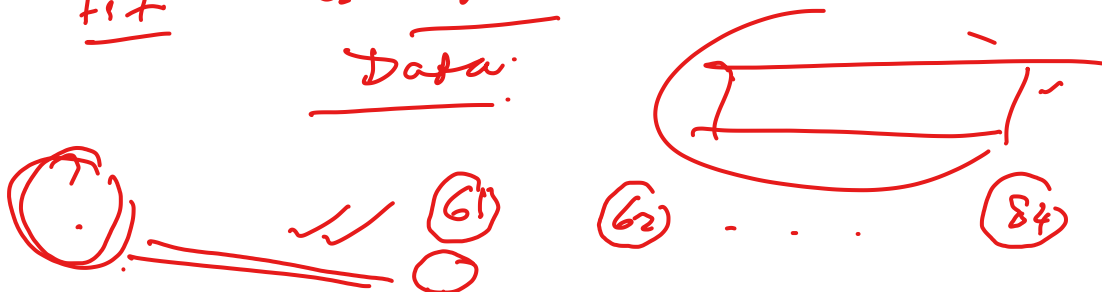
70% of 84 = 60 months
↓
Training

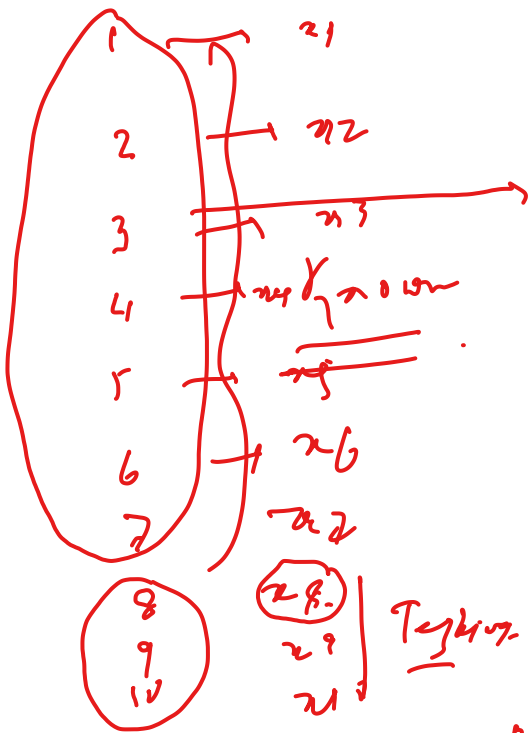
Training & Testing.

✓ 70%.	30%.
80%.	20%.
65%.	35%.
60%.	40%.

24 months for Testing.

Fit or Train model on 60 months
Data:





$$x_t = 0.3 + 0.5 x_{t-1}$$

(Aggins)

$$x_1 = 0.3 + 0.5 x_0$$

$$x_2 = 0.3 + 0.5 x_1$$

$$x_8 = 0.3 + 0.5 x_7$$

Bootstrapping validation of machine learning

- 1) Recurrent validation
- 2) K-fold validation
- 3) LOOCV [Leave one out cross validation]

Data analysis.

K-fold Fold. $K=5$ $K=10$

$$n = 100$$

Fold 1	—	20
2	—	20
3	—	20
4	—	20
5	—	20

Err { Training Step 1 $\rightarrow$ Fold 1 + Fold 2 + Fold 3 + Fold 4 = 80%
 Testing $\rightarrow$ Fold 5

Err ~ Step 2 Fold 2 + Fold 3 + Fold 4 + Fold 5 = 80%
 Testing $\rightarrow$ Fold 1.
 Err $\hookrightarrow$ Step 3 $\rightarrow$ Fold 1.
 Err $\hookrightarrow$ Step 4 $\rightarrow$ Fold 2 + Fold 4 + Fold 1.
 Err $\hookrightarrow$ Step 5 $\rightarrow$ Fold 3 + Fold 5 + Fold 1.
 Err $\hookrightarrow$ Step 6 $\rightarrow$ Fold 4.

$$\sigma = 123.$$

$$\begin{array}{r} 5. \text{ fold} \\ 123/5. \quad 23.0 \\ \hline 24.6 \end{array}$$

$$\begin{array}{r} \text{Fold 1} \quad 24 \\ 2 \quad 24 \\ 3 \quad 24 \\ 4 \quad 24 \end{array} \left. \vphantom{\begin{array}{r} \text{Fold 1} \\ 2 \\ 3 \\ 4 \end{array}} \right\} \rightarrow 27$$

y = observed value.

$\hat{y}$ = model.

$$\text{Err} = (y - \hat{y})^2.$$

$$[(\text{Err})^2] = \sum (y - \hat{y})^2.$$

known (y)

	x_1	x_2	(y)	$(y - \hat{y})$
2	1	2	✓	-
4	3	3	✓	-
6	5	9	✓	-
8	7	15	✓	-
10	9	20	✓	-

$$\text{Cost } E = b_0 + b_1 x_1 + b_2 x_2$$

$$= 2 + 0.5 x_1 + 0.3 x_2$$

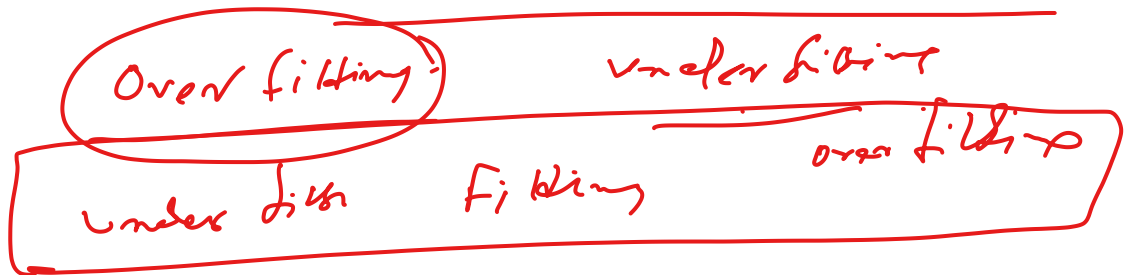
$$\frac{\sum (y - \hat{y})^2}{n}$$

$$MSE = \frac{\sum (y - \hat{y})^2}{n}$$

$$RMSE = \sqrt{\text{Mean Squared Error}}$$

$$RMSE = \sqrt{MSE}$$

MSE & RMSE for Training & Testing.



Goodness

✓ Goodness fit.

Correlation coefficient R^2

Model 1

Bayesian dist

✓ AIC BIC SIC

Akaike information criteria

AIC in best model

Loop cv.

Leave one out cross validation

60 months

~~RMSE or MRE~~

ROR of 60 months

AROR

60 months

5.9

AROR

$\bar{x} = \dots$

1
2
3
4
5

$\bar{x}_1 =$

$\bar{x}_2 =$

$\bar{x}_3 =$

$\bar{x}_4 =$

$\bar{x}_5 =$

Loop

$$\bar{x} = \frac{\bar{x}_1 + \bar{x}_2 + \bar{x}_3 + \bar{x}_4 + \bar{x}_5}{5}$$

based on 5 obs.

Average to minimize error

Also v4. [v ~ Imp]

Analysis 7 variables

Avg. Prediction Error = Avg. Reducible error + Avg. Irreducible error

Measurement error

Control

Inherent

Not in control

obj) of Data Analysis.

Data Sample

One. Day
Drive

✓ 1 run.

1) Between
m/c

	T ₁	T ₂	T ₃	T ₄	T ₅
Machine 1	P ₁₁	P ₁₂	P ₁₃	P ₁₄	P ₁₅
Machine 2	P ₂₁	P ₂₂	P ₂₃	P ₂₄	P ₂₅
Machine 3	P ₃₁	P ₃₂	P ₃₃	P ₃₄	P ₃₅

2) Within

Contrast.

$$\text{Problem} = f(Y/D)$$

Two Day Drive

Fixed inter.

machine	01	02	03
M ₁	<u>Production</u>		
M ₂			
M ₃			

$$\text{Production} = f(Y/D)$$

$$\text{OP} = f(Y/D)$$

$$\text{Production} = f(Y/C, OP, Y/C \times OP)$$

Two Way Drive.

84 Months.

Factor

7 years.

Banking

36 Bank.

(2) Public

(1) Private

4 Public

4 Private

	$\bar{y}_1$	$\bar{y}_2$	...	$\bar{y}_7$
Bank 1	0	0	.	0
Bank 2	0	0	.	.
Bank 3	0	0	.	0
Bank 4	0	0	0	0

If no of Banks $> 2 \Rightarrow$ ANOVA ✓
 if the obs. follow normal dist.

Non-Parametric
Kruskal Wallis Test

no of Banks = 2 $\Rightarrow$ t-Test ()
Man-Wilney U-Test

(obj) $\therefore$ All Banks are equally efficient
 if not, rank the bank.
writing ANOVA.

Appl. Ans.

✓ $H_0: \mu_{B_1} = \mu_{B_2} = \mu_{B_3} = \mu_{B_4}$
 ✓ H_1 : At least two banks are
 not equally efficient

If H_0 is accepted then
Statistical mathematical there is a difference
 of their sample means =

If it is rejected. then we can easily find their rank using Paired - t - Test (Tukey)

Source	Sum of Square	Df	Mean Sum of Squar	F	p-value
Between					(0.05)
Within					
Total					

✓ It is rejected

To rank the Banks as apply Post hoc. Test

G_{r1}	G_{r2}	G_{r3}

$$\bar{\pi}_1 < \bar{\pi}_2 < \bar{\pi}_3$$

Post hoc

Later homogeneity comparison

- G_{r-3} - Rank 1
- G_{r-2} - Rank 2
- G_{r-1} - Rank 3

$$G_{r1} = \begin{pmatrix} G_{r2} \\ G_{r3} \end{pmatrix}$$

$$G_{r2} = G_{r3}$$

W
O

~

G_{r1}	G_{r2}
	G_{r3}

Dimension
reduction

