

✓ Univariate

four point

five point

Mean, S.D. skewness

& kurtosis

min, q1, q2, q3, max

Export

EDA

Exploring Data Analysis

Descriptive

Diagnostic

Predictive

Prescriptive

freq.

non freq.

Primary

Secondary

Random experiment

Coin

1) Probability

uncertain

Prob.

2) Conditional Prob.

3) Bayes' Th.

4) Random variable

Discrete

Continuous

Discrete R.V.

1) Countable Finite

2) Countable infinite

20 coins are tossed  
How many heads

✓ No. of mobile call.  
✓ No. of deaths.  
✓ No. of births

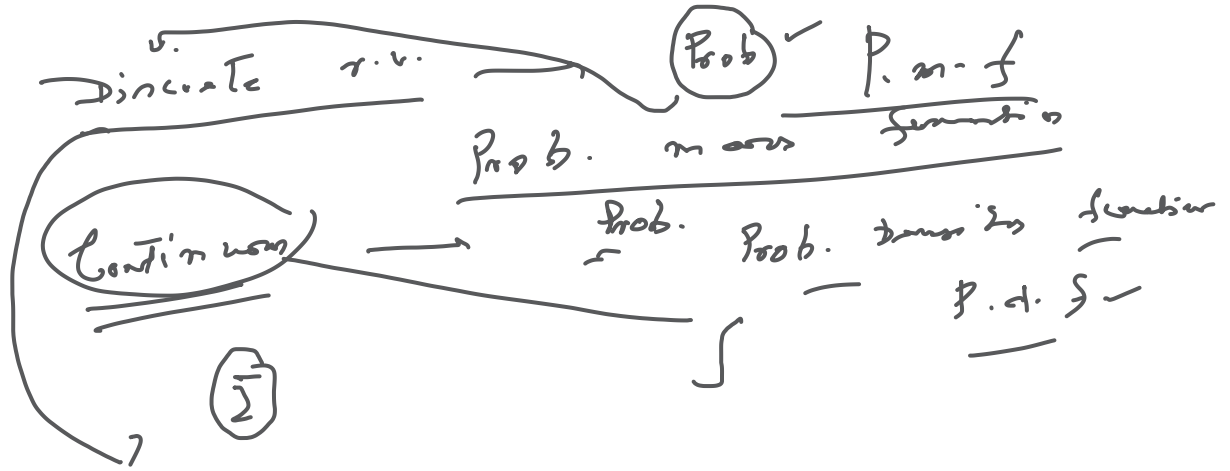
✓ Continuous R.V.

Age

Length, weight, income, uncountable

0-1

0.1, 0.01, 0.001



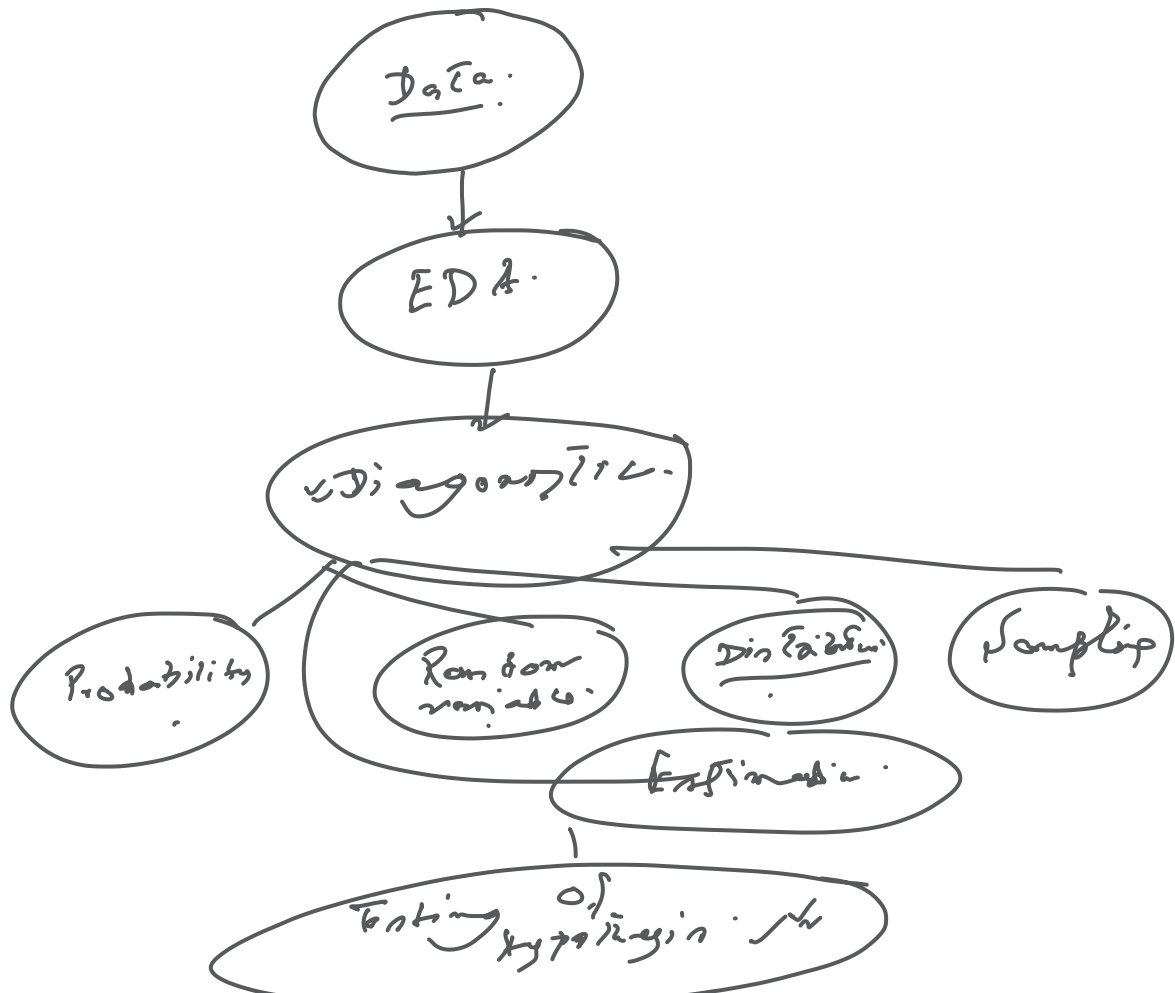
Most Most imp  
Pattern of Data



#1- To estimate population parameter  
 with the help of sample  
 statistic.

To minimize error for estimation.

✓ Estimation



Derive a Distribution

|                 |                   |                          |
|-----------------|-------------------|--------------------------|
| <u>Sampling</u> | 1) t-distribution | 2) $\chi^2$ (chi) square |
|                 | 3) F-distribution |                          |

✓ Analysis of variance ✓

Two population & more than two pop?

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Multivariate analysis

Feature Selection

Sample size. 1,13,000

|                  |         |     |
|------------------|---------|-----|
| no. of variables | Nominal | DO5 |
|                  | ordinal |     |
|                  | Scale   |     |

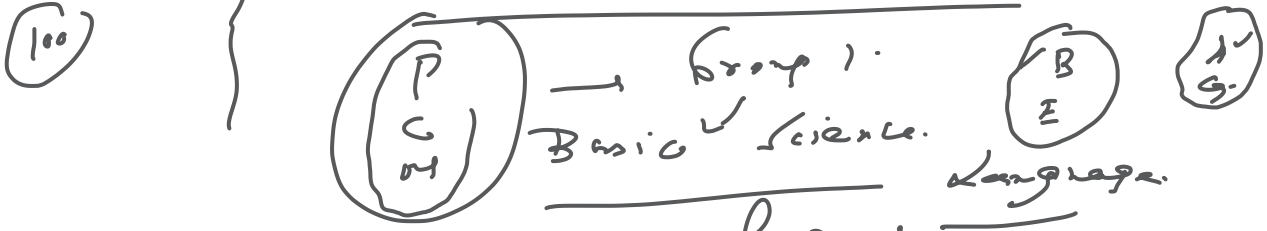
(181)

1,13,000 - row  
(181) - col

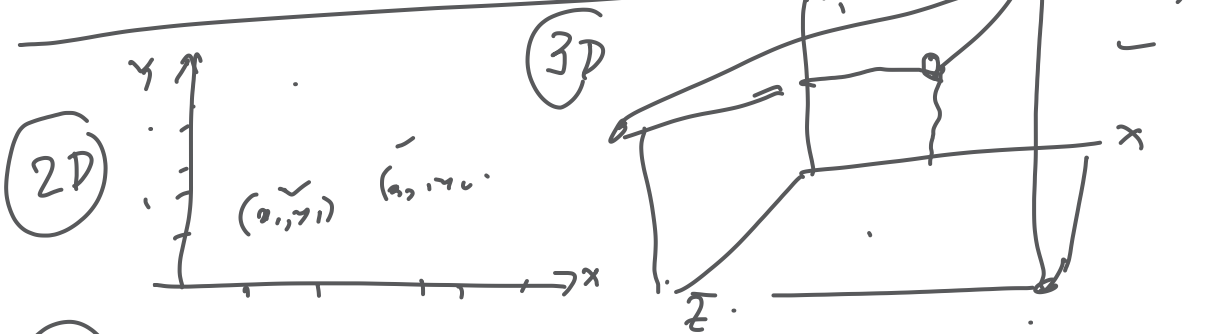
- ① Some variables / Some attributes are not imp.  $\Rightarrow$  Discard using some method.
- ② Some variables / attributes can be homogeneous or they are highly correlated with each other.

Some variables  $\rightarrow$  P C M B E H G.

underlying construct



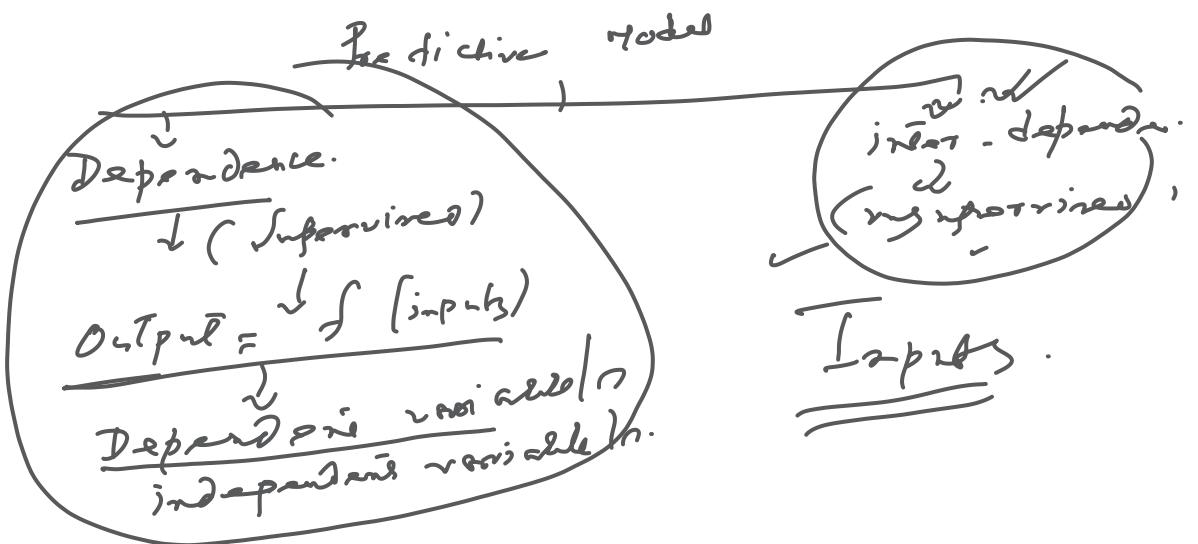
Dimension Reduction.



④

Predictive model.

- ① Cross Sectional. ② Longitudinal. ③ Panel.



✓ (1) Regression / Time Series

Classification

(2) ~~the~~ PCA, Factor  
analysis  
Cluster Analysis

Prescriptive

## Optimization

Local → Global

Witz

Try to optimize - error

$$\left\{ \begin{array}{l} p = \frac{\text{population}}{\text{sample}} \\ s = \end{array} \right.$$

$E =$  Energy gap in the universe -  
-10,  $10^{-9}$ .

Stocks & Bonds

| Year | USA | Taper | vs | India | China |
|------|-----|-------|----|-------|-------|
| 2021 | ✓   | ✓     | ✓  | ✓     | ✓     |
| 2022 |     |       |    |       |       |

Countries | Stock Booms ✓ | Probability

(Crown) → ✓

- ① Trial. ② Event ③ Equally outcome  
event ④ Exhaustive cases ⑤ Equally likely

Turning a coin (or die) - Trial.  
 Outcome Head. Tail.

Possible Outcomes

coin {H, T}  
 die {1, ..., 6}  
 {1, ..., 52}

Def<sup>n</sup> Prob. =  $\frac{\text{Favorable no. of Outcomes of an event}}{\text{Total no. of Outcomes of an event}}$

voting  $N = 100$

|    |       |                           |   |
|----|-------|---------------------------|---|
|    |       | A                         | B |
| 60 | Favor | $P(A) = \frac{60}{100}$ ✓ |   |
| 40 | "     | $P(B) = \frac{40}{100}$ ✓ |   |

$P + Q = 1$

Total Prob = 1 ✓

$Prob = \frac{x}{n}$

$0 < P < 1$

✓  $P = 0 \Rightarrow$  Impossible event  
Certain event  
 $P = 1 \Rightarrow$

Uncertain event  $< 1$

|     |    |   |                         |
|-----|----|---|-------------------------|
| 100 | 60 | A | $P(A) = \frac{60}{100}$ |
|     | 40 | B | $P(B) = \frac{40}{100}$ |

$P(A) + P(B) = 1$

$$N = \{1, 2, \dots, 10\} \quad A = \{1, 2, 3, 4, 5\}$$

$\approx 10$

$$B = \{3, 4, 5, 6\}$$

$n(A) = \text{cardinality}$   
 $\# A = \text{members}$   
 in the set 4.  
 $5 \checkmark$

$$n(B) = 4 \checkmark$$

$$A \cup B = \{1, 2, 3, 4, 5, 6\}$$

$$n(A \cup B) = 6$$

$$A \cap B = \{3, 4, 5\} \quad n(A \cap B) = 3 \checkmark$$

$$n(A \cup B) = n(A) + n(B) - n(A \cap B)$$

$$6 = 5 + 4 - 3$$

$$n(A \cup B) = \frac{n(A)}{N} + \frac{n(B)}{N} - \frac{n(A \cap B)}{N}$$

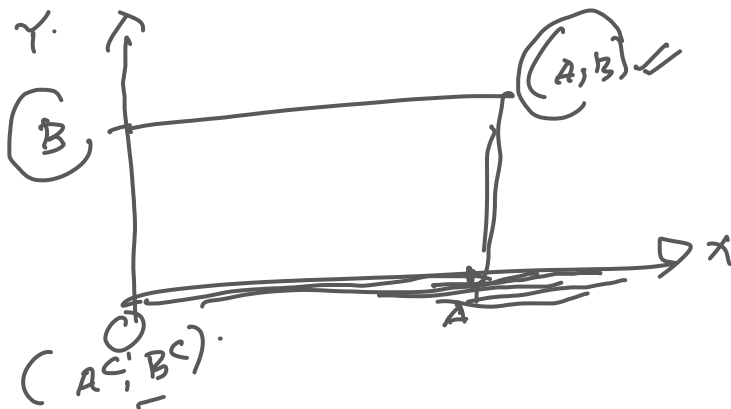
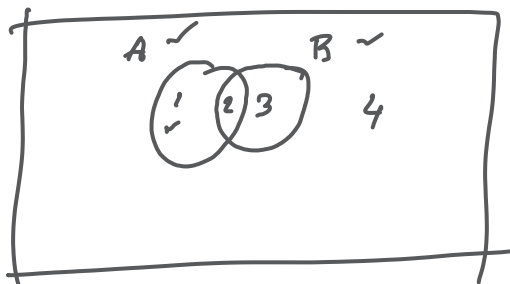
Favorable  
no of  
cases

$$\Rightarrow P(A \cup B) = P(A) + P(B) - P(A \cap B)$$

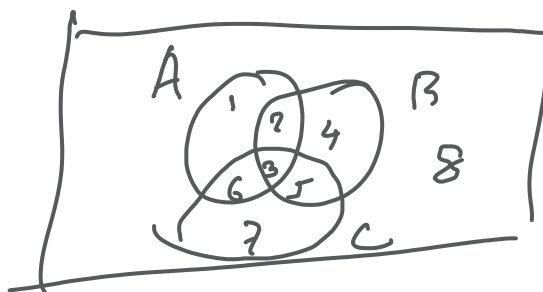
when A & B are mutually exclusive events

A B.

only A: 1 =  $n(A \cap B^c)$   
 A & B: 2 =  $n(A \cap B)$   
 both  
 only B: 3 =  $n(A^c \cap B)$   
 no A  
 & no B: 4 =  $n(A^c \cap B^c)$



~~$P(A \cap B) + P$~~   
 1 =  $n(A \cap B^c)$   
 2 =  $n(A \cap B)$   
 3 =  $n(A^c \cap B)$   
 4 =  $n(A^c \cap B^c)$



$$5 = a(A^c B^c C) \quad 6 = a(A B^c C) \quad 7 = a(A^c B^c C)$$

$$8 = a(A^c B^c C)$$

when there are two sets,  
 how many points =  $2^2 = 4$ .

when there are three sets =  $2^3 = 8$ .

$$\frac{\text{p. sets}}{\text{p. variables}} = 2^p$$

$$\underline{p=20} \quad 2^{20} = 10,48,576$$

Dimension reduction

Current Salary depending on:  
 { Beginning sal, Prev. Exp, Specialization,  
 opening role sticker  
 (4)  $2^4 = 16$

Stock - MKT

Stock Price

Sensor =  $f(\text{Gold Price, Dollar, RR, FDI, Foreign, Foreign})$

$$2^6 = (64)$$

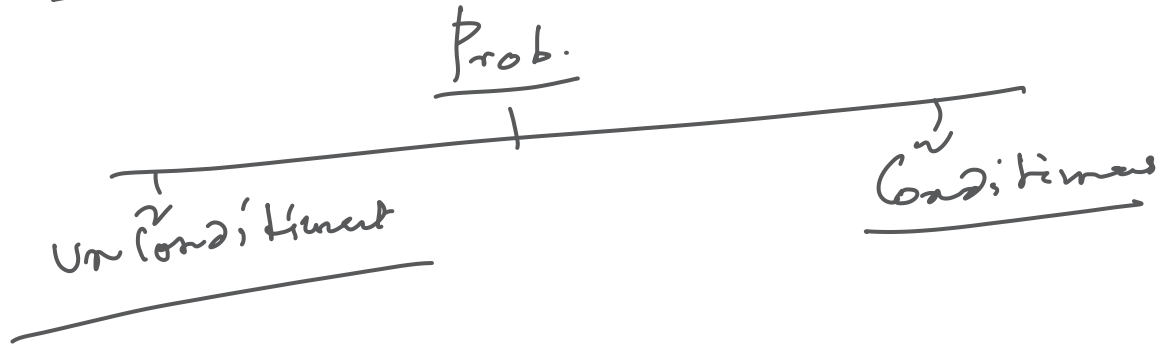
Covid RTPCR.

| Age group  | Total intake | No. of deaths |
|------------|--------------|---------------|
| G1 < 30    | 5000         | 5             |
| G2 30 - 50 | 3000         | 15            |
| G3 > 50    | 2000         | 40            |
|            | N = 10000    | 60            |

$$P(D) = \frac{60}{10000} = 0.006$$

$$\begin{cases} P(D/G_1) = 5/5000 = 0.1\% \\ P(D/G_2) = 15/3000 = 0.2\% \\ P(D/G_3) = 40/2000 = 2\% \end{cases}$$

Conditional



Stock A.

60 months

$\checkmark$  min  $\phi_1, \phi_2, \phi_3, \dots$

$\phi_1 = 5$

$\phi_2 = 15$

$\phi_3 = 30$

$\phi_4 = 10$

$\phi_1 + \phi_2 + \phi_3 + \phi_4 = 60$

$P_1 + P_2 + P_3 + P_4 = 1$

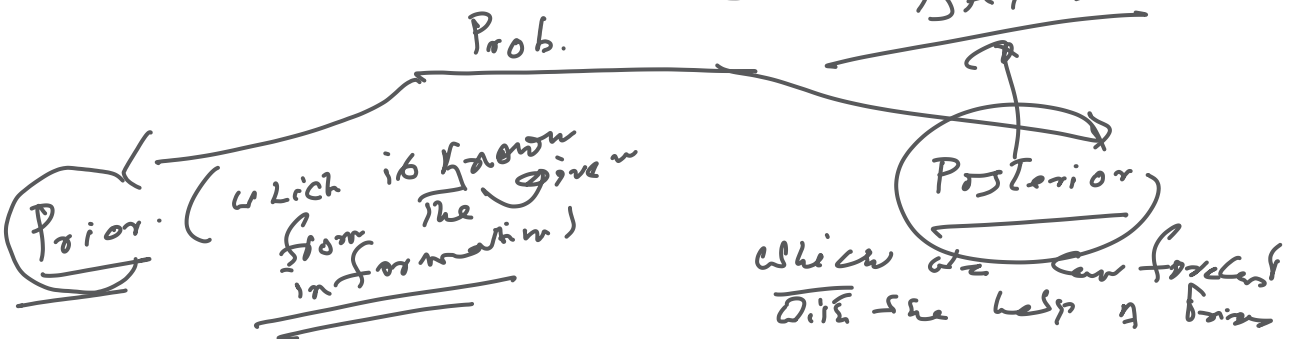
$p(G_1) = 5/60$

$p(G_2) = 15/60 = 1/4$

$p(G_3) = 30/60 = 1/2$

$p(G_4) = 10/60 = 1/6$

BAYE'S



~~B members:~~

$$\begin{array}{r} 75 \\ 108 \cdot \\ \hline 163 \cdot \\ \textcircled{17} \end{array}$$

no of members = 2.  
 $\therefore$  Total no of subsets  
 $= 2^2 = 4$

